

Large Gravitational Wave Background Signals in Electroweak Baryogenesis Scenarios

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The bubble wall velocity in an electroweak first order phase transition is a key quantity both for electroweak baryogenesis and for the production of a stochastic background of gravitational waves that may be probed in the future through gravitational wave experiments like LISA or BBO. We show that, contrary to the conclusion drawn from previous studies, it is actually possible to generate a potentially large gravitational wave signal while satisfying the requirements for viable electroweak baryogenesis, once the effects of the hydrodynamics of bubble growth are taken into account. Then, the observation of a large gravitational wave background from the electroweak phase transition would not necessarily rule out electroweak baryogenesis as the mechanism having generated the observed baryon asymmetry of the universe.

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I. INTRODUCTION

The study of bubble growth in cosmological first order phase transitions is very relevant for many phenomena having possibly occurred in the early universe such as electroweak baryogenesis [1, 2] or the production of a stochastic background of gravitational waves [3–5]. A first order phase transition proceeds by bubble nucleation and expansion, and the velocity of the expanding bubble walls plays an essential role both in electroweak baryogenesis and in gravitational wave production, since the efficiency of both processes strongly depends on its value.

Treatments of the bubble wall velocity generally assume that friction from the plasma balances the initial pressure difference that drives the bubble expansion, so that the wall reaches a constant speed after a short period of acceleration. Assuming that the free energy of the Higgs field is released into the plasma, a hydrodynamic treatment of the plasma can be used to determine the fluid motion [6, 7], but this approach leaves the wall velocity as a free parameter as long as the microscopic mechanism of friction is unknown. Ultimately, the wall velocity can be fixed using the equation of motion for the Higgs field, that takes into account the friction of the plasma [8, 9].

However, successful electroweak baryogenesis and sizable gravitational wave production require very different wall velocities. The electroweak baryogenesis mechanism is based on the interaction between the expanding bubble wall and the plasma in front of it, leading to a CP asymmetric reflection on the wall of certain particle species, and the subsequent diffusion of these particle asymmetries into the plasma in front of the bubble wall [2], where sphalerons are active and capable of converting the CP asymmetry into a net baryon number. Then the generated baryon number is carried into the broken phase as the wall passes by (where it stays frozen if the sphaleron processes are sufficiently suppressed in the broken phase). In order for this whole mechanism to be effective the diffusion timescale has to be smaller than the time the wall takes to sweep through the plasma just in front (other-

wise diffusion is ineffective and the generation of baryon number is strongly suppressed), and this puts an upper bound on the relative velocity between the wall and the plasma in front $V \lesssim D/L_w \sim 0.15 - 0.3$ (being D a certain diffusion constant and L_w the wall thickness) [2]. Moreover, it is generally stated that subsonic wall velocities are always needed, because effective diffusion cannot take place for supersonic walls. On the other hand, fast moving walls are essential for the production of a sizable amount of gravitational radiation in bubble collisions [4, 5, 10–12], or turbulence in the plasma [13, 14]. In particular, for bubble collisions the gravitational wave amplitude is roughly proportional to V_w^3 [10, 11], with an extra implicit V_w -dependence through the efficiency coefficient κ for transforming the available energy from the phase transition into plasma bulk motion (which is in turn responsible for the generation of the gravitational wave background during the bubble collisions [5, 15]), and this dependence further suppresses the gravitational wave signal for small wall velocities (this suppression also affects the gravitational wave signal generated from turbulence). All this has established the common lore that both phenomena cannot happen in the same scenario.

In the Standard Model, and for values of the Higgs mass above the LEP bound $M_h > 114.4$ GeV [20], the electroweak phase transition is found not to be of first order, but rather a smooth cross-over [21]. However, there are many possible theories beyond the Standard Model in which the electroweak phase transition may naturally be of first order, such as extensions of the MSSM [22–24] (in the MSSM itself, the region of parameter space where a first order phase transition leading to electroweak baryogenesis is achieved is currently very tightly constrained [25]), Two-Higgs-Doublet models [26–29], singlet field extensions of the Standard Model [30–34], composite Higgs models and others. Also, in [35] the electroweak phase transition was studied for the Standard Model considered as an effective theory with a low cut-off, finding that the inclusion of higher dimensional operators in the Higgs potential may give rise to a rather strong first order phase transition. As it has been discussed above, for these or

any other model leading to a first order electroweak phase transition, the value of the velocity of the expanding bubbles is a key parameter for the study of both electroweak baryogenesis and gravitational wave production at the phase transition. For the case of the MSSM the value of V_w was found to be quite small over all the available parameter space [36], but it is expected that it may be much larger in many of the models discussed above, since the electroweak phase transition in those cases is much more strongly first order, since the wall velocity increases with the strength of the phase transition [9].

Here we will show that in contrast to the case of gravitational wave production, where the relevant velocity is indeed the speed of the wall V_w , in electroweak baryogenesis the relevant velocity (being the relative velocity between the bubble wall and the plasma just in front the wall v_+) is in general lower than V_w , and this effect becomes more important as the phase transition gets stronger. Then, it is possible to have a sizable gravitational wave production (through a relatively large V_w , a natural possibility in many of the scenarios beyond the Standard Model mentioned above, where the electroweak phase transition can be strongly first order) while the electroweak baryogenesis mechanism is still effective (v_+ is sufficiently low).

This article will be organized as follows: In section 2 a summary of the hydrodynamic analysis of bubble expansion is given. Then, in section 3 the use of v_+ instead of V_w as relevant velocity for electroweak baryogenesis is motivated, and in section 4 it is shown that $v_+ < V_w$ (and $v_+ \ll V_w$ for strong transitions). In section 5 the gravitational wave amplitude in viable electroweak baryogenesis scenarios is obtained, and we conclude in section 6.

II. HYDRODYNAMIC RELATIONS.

The hydrodynamic analysis of the system consisting on the Bubble wall and the plasma surrounding it [6, 7, 15] rests on two basic assumptions: energy-momentum conservation in the system and local thermal equilibrium (LTE) in the plasma. This last assumption is reasonable since local equilibration due to the interactions between the particle species in the thermal plasma is much faster than the actual macroscopic movement of the plasma. Local thermal equilibrium is also crucial for the consistency of the fluid approximation applied in electroweak baryogenesis computations (see [2]).

The energy-momentum tensor of the Higgs field ϕ is given by

$$T_{\mu\nu}^\phi = \partial_\mu \phi \partial_\nu \phi - g_{\mu\nu} \left[\frac{1}{2} \partial_\rho \phi \partial^\rho \phi - V_0(\phi) \right], \quad (1)$$

where $V_0(\phi)$ is the renormalized vacuum potential. If the plasma is locally in equilibrium its energy-momentum tensor can be parametrized as

$$T_{\mu\nu}^{\text{plasma}} = w u_\mu u_\nu - g_{\mu\nu} p, \quad (2)$$

where w and p are the plasma enthalpy and pressure, respectively. The quantity u_μ is the four-velocity field of the plasma, related to the three-velocity \mathbf{v} by $u_\mu = (\gamma, \gamma \mathbf{v})$. The enthalpy w , the entropy density σ and the energy density e are defined by

$$w \equiv T \frac{\partial p}{\partial T}, \quad \sigma \equiv \frac{\partial p}{\partial T}, \quad e \equiv T \frac{\partial p}{\partial T} - p, \quad (3)$$

where T is the temperature of the plasma. Conservation of energy-momentum is given by $\partial^\mu T_{\mu\nu}^\phi + \partial^\mu T_{\mu\nu}^{\text{plasma}} = 0$. Since we are interested in a system where the bubble expands at a constant speed, energy-momentum conservation reads in the wall frame (assuming no time dependence, and with the wall and fluid velocities aligned in the z direction) $\partial_z T^{zz} = \partial_z T^{z0} = 0$. Integrating these equations across the wall and denoting the phases in front and behind by subscripts $+$ (symmetric phase) and $-$ (broken phase) one obtains the matching equations in the wall frame:

$$\begin{aligned} w_+ v_+^2 \gamma_+^2 + p_+ &= w_- v_-^2 \gamma_-^2 + p_- \\ w_+ v_+ \gamma_+^2 &= w_- v_- \gamma_-^2 \end{aligned} \quad (4)$$

From these equations we can obtain the relations [7]

$$v_+ v_- = \frac{p_+ - p_-}{e_+ - e_-}, \quad \frac{v_+}{v_-} = \frac{e_- + p_+}{e_+ + p_-}. \quad (5)$$

In order to proceed further, one needs to know the equation of state (EoS) for the plasma. A parametrization that accounts for deviations from the so-called bag EoS (usually used in hydrodynamical studies of phase transitions in the early universe [5, 7]) is (see [15])

$$p_+ = \frac{1}{3} a_+ T_+^4 \quad e_+ = a_+ T_+^4 \quad (6)$$

$$\begin{aligned} p_- &= \frac{1}{3} a_- T_-^4 + \epsilon \equiv a_+ T_+^4 \left(\frac{1}{3r} + \alpha_+ \right) \\ e_- &= a_- T_-^4 - \epsilon \equiv a_+ T_+^4 \left(\frac{1}{r} - \alpha_+ \right) \end{aligned} \quad (7)$$

where we have defined $\alpha_+ \equiv \frac{\epsilon}{a_+ T_+^4}$ and $r \equiv \frac{a_+ T_+^4}{a_- T_-^4}$. The quantity α_+ is approximately the ratio of vacuum energy difference to thermal energy in front of the wall, and characterizes the strength of the phase transition (the larger α_+ the stronger the transition), and a_\pm are related to the number of relativistic d.o.f in the symmetric and broken phases. Using (6) and (7) we can write the relations (5) as

$$v_+ v_- = \frac{1 - (1 - 3\alpha_+)r}{3 - 3(1 + \alpha_+)r}, \quad \frac{v_+}{v_-} = \frac{3 + (1 - 3\alpha_+)r}{1 + 3(1 + \alpha_+)r} \quad (8)$$

The two equations (8) can be combined to give

$$v_+ = \frac{1}{1 + \alpha_+} \left[\left(\frac{v_-}{2} + \frac{1}{6v_-} \right) \pm \sqrt{\left(\frac{v_-}{2} + \frac{1}{6v_-} \right)^2 + \alpha_+^2 + \frac{2}{3}\alpha_+ - \frac{1}{3}} \right] \quad (9)$$

so that there are two branches of solutions, corresponding to the \pm signs in (9).

In a concrete model where $p = -\mathcal{F}$ (the free energy or finite-temperature effective potential) is known, the thermodynamic potentials can be calculated in the two phases and the temperature T_N at which the phase transition happens is determined using standard techniques [16]. Still, there are three unknown quantities (T_- , v_+ and v_-) and two equations (5), so up to this point all hydrodynamically viable solutions are parametrized by one parameter, usually chosen to be the wall velocity V_w .

Next, we briefly review the solutions of the plasma velocity v [15, 17]. Applying energy-momentum conservation in the plasma $\partial^\mu T_{\mu\nu}^{\text{plasma}} = 0$ (far from the wall $T_{\mu\nu}^\phi$ just gives a constant background that plays no role in the energy-momentum conservation), we obtain a set of hydrodynamic equations. Since there is no intrinsic macroscopic length scale in the system, solutions to these equations are self-similar and only depend on $\xi = r/t$, with r being the radial coordinate of the bubble and t the time since nucleation. The plasma then fulfills the equations

$$2\frac{v}{\xi} = \gamma^2(1 - v\xi) \left[\frac{\mu^2}{c_s^2} - 1 \right] \partial_\xi v$$

$$\frac{\partial_\xi w}{w} = 4\gamma^2 \mu(\xi, v) \partial_\xi v \quad (10)$$

where $c_s = 1/\sqrt{3}$ denotes the velocity of sound in the plasma and $\mu(\xi, v)$ is the Lorentz-transformed fluid velocity $\mu(\xi, v) = \frac{\xi - v}{1 - \xi v}$. Generally, there are three different types of solutions to (10) with the boundary conditions (9) [15, 17]: detonations, deflagrations and hybrid solutions. In detonations the bubble wall expands at supersonic velocities and the vacuum energy of the Higgs leads to a rarefaction wave behind the wall, while the plasma in front is at rest. In this case, the wall velocity is $V_w = v_+ > v_-$, and therefore detonations are identified with the $+$ branch of solutions in (9). In deflagrations, the plasma is mostly affected by reflection of particles at the bubble wall and a compression wave builds up in front of the wall while the plasma behind is at rest. In this case, the wall velocity is identified with $V_w = v_- > v_+$, corresponding to the $-$ branch of solutions in (9). While “pure” deflagrations are subsonic, the hybrid case occurs for supersonic deflagrations where both effects (compression and rarefaction wave) are present. From now on we will focus on deflagrations and hybrids since for them $V_w > v_+$. Also, in this case $T_+ > T_N$, and so $\alpha_+ < \alpha_N \equiv \frac{\epsilon}{a_+ T_N^4}$ (being α_N the actual measure of the strenght of the phase transition).

III. v_+ VS V_w IN ELECTROWEAK BARYOGENESIS.

Consider the evolution of a plasma volume element as the compression front and bubble wall reach it and pass by, in the case of a deflagration (Figure 1). The element is initially at rest (its position $r = \text{cte}$), and as it enters the compression wave it acquires a velocity, that grows until reaching $v(V_w) = \frac{V_w - v_+}{1 - V_w v_+}$ close to the bubble wall. Then, due to the compression wave, the relative velocity between the wall and the volume element just in front of it is v_+ independently from the details of the electroweak baryogenesis mechanism close to the wall, just relying on LTE applying all over the compression wave. In the electroweak baryogenesis analysis the relevant velocity is the perturbation \bar{V} with respect to the background velocity of the plasma v_+ . However, in [2] (and subsequent electroweak baryogenesis studies) the background velocity of the plasma was taken to be V_w , neglecting hydrodynamics. We find that in the presence of a compression wave and in the wall reference frame, the velocity of the plasma should be $V = -v_+ + \bar{V}$ instead of $V = -V_w + \bar{V}$, and so the dependence of the electroweak baryogenesis mechanism on the wall velocity V_w extracted from [2] is actually a dependence on v_+ . The same argument applies to the upper bound on V_w from [2] from the requirement of effective diffusion of the CP asymmetric current in front of the wall. The bound should now be regarded as $v_+ \lesssim D/L_w \sim 0.15 - 0.3$ (the wall thickness $L_w \sim (15 - 40)/T$ and the diffusion constant $D \sim 5/T$ [2]).

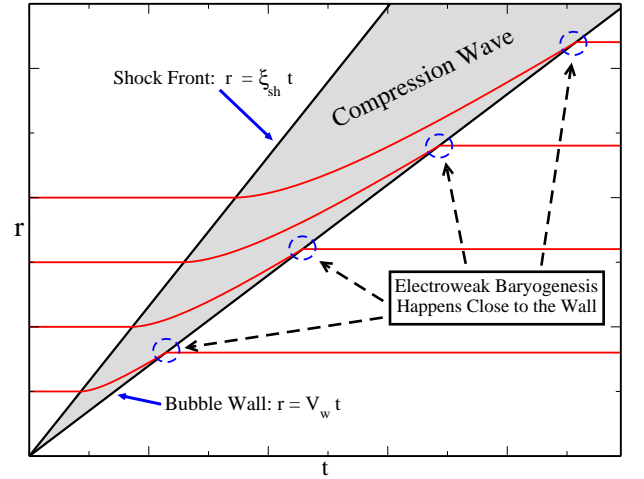


FIG. 1: Movement of plasma volume elements with time.

IV. DEPARTURE OF v_+ FROM V_w .

In the presence of a compression wave (deflagrations and hybrid solutions) it is seen from (9) and (10) that $V_w > v_+$. For weak first order phase transitions ($\alpha_N \ll$

1) one has $v_+ \simeq V_w$ from (9) and the effect of considering v_+ instead of V_w as the relevant velocity for electroweak baryogenesis is small. However, as α_N gets larger (always keeping $\alpha_+ < 1/3$ [15]) and the phase transition gets stronger, v_+ progressively departs from V_w , eventually reaching $v_+ \ll V_w$ for very strong phase transitions. This is shown in Figure 2, where $v_+(V_w)$ is plotted for increasing values of α_N . Then, for rather strong phase transitions, v_+ can be kept small enough to satisfy the diffusion upper bound for electroweak baryogenesis $v_+ \lesssim 0.15 - 0.3$ with a rather large V_w ($V_w \sim c_s$ for deflagrations or even $V_w > c_s$ for hybrid solutions).

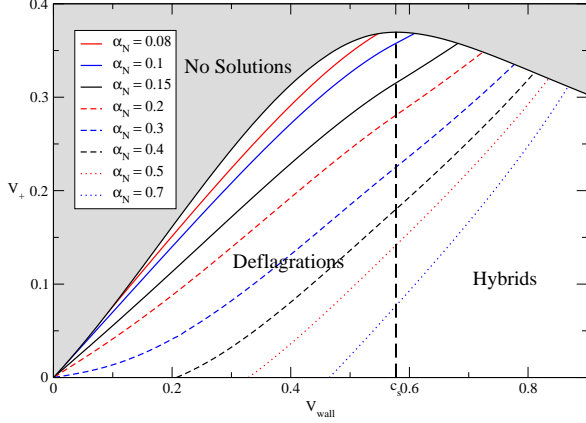


FIG. 2: Relation $v_+(\alpha_N, V_w)$.

In Figure 3 the region in the parameter space of α_N and V_w compatible with electroweak baryogenesis (for various values of the upper bound on v_+) is shown. For large α_N and small V_w , $\alpha_+ > \frac{1}{3}$ and no solutions exist [15]. Also, for small α_N there is a maximum value V_w can take with positive plasma friction [18], and α_N has to be larger than a critical value α_c for bubble expansion to be possible ($\alpha_c \simeq 0.05$ for $a_-/a_+ = 0.85$) [15, 18].

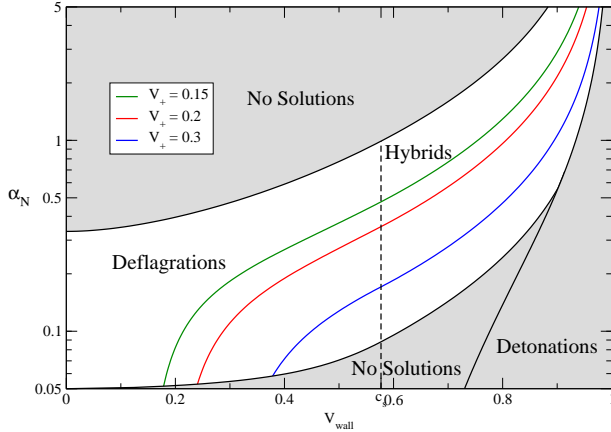


FIG. 3: Regions in the (V_w, α_N) plane compatible with $v_+ < 0.15$, $v_+ < 0.2$ and $v_+ < 0.3$ (region above each line).

V. HOW BIG CAN THE GRAVITATIONAL WAVE SIGNAL BE?

Here we will concentrate on production of gravitational waves through bubble collisions during an electroweak first order phase transition (the analysis can be extended to the case of turbulence, with similar conclusions). The amplitude and peak frequency of the generated stochastic spectrum are [11] (see also [5, 10]):

$$\Omega_{GW} h^2(f_{coll}) \simeq 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right)^2 (\kappa(\alpha_N, V_w))^2 \left(\frac{\alpha_N}{1 + \alpha_N} \right)^2 \frac{1.84 V_w^3}{0.42 + V_w^2} \quad (11)$$

$$f_{coll} \simeq 10^{-2} \text{ mHz} \left(\frac{g_*}{100} \right)^{\frac{1}{6}} \left(\frac{T}{100 \text{ GeV}} \right)^2 \frac{\beta}{H_*} \frac{1.2}{1.8 + V_w^2} \quad (12)$$

and the spectrum grows as f^3 for frequencies smaller than f_{coll} [5, 10] and falls off as f^{-1} for large frequencies [11]. Typically $\beta/H_* \sim 100$ [19] and for the electroweak phase transition $T \sim 100 \text{ GeV}$ and $g_* \sim 100$. Then, if viable electroweak baryogenesis would require $V_w < 0.15 - 0.3$, this would suppress the gravitational wave amplitude both explicitly and through the efficiency coefficient $\kappa(\alpha_N, V_w)$ dependence even for rather strong phase transitions ($\alpha_N \sim \mathcal{O}(0.1 - 0.2)$), making the gravitational wave signal in scenarios where electroweak baryogenesis is possible undetectable both at LISA and BBO (blue lines in Figure 4). Moreover, for very strong transitions ($\alpha_N \sim \mathcal{O}(1)$) it would be impossible to satisfy the bound $V_w < 0.15 - 0.3$ and electroweak baryogenesis would simply not be possible.

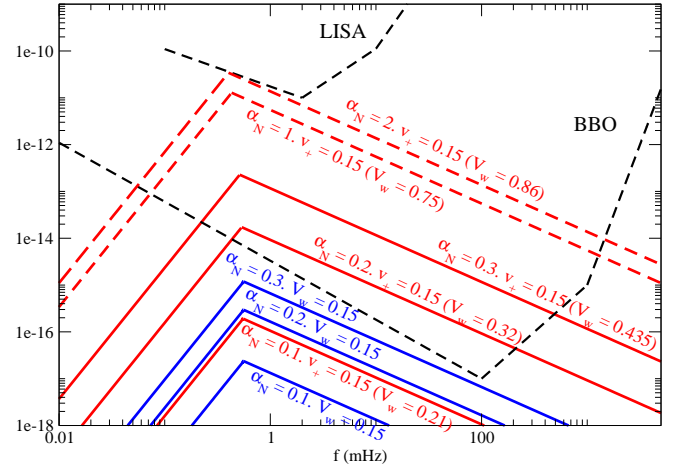


FIG. 4: $\Omega_{GW} h^2(f)$ for various values of α_N and $V_w = 0.15$ (blue lines) or $v_+ = 0.15$ (red lines).

However, since the electroweak baryogenesis bound actually applies to v_+ , the gravitational wave signal amplitude for a scenario where the bound is satisfied gets

enhanced by 2-3 orders of magnitude with respect to the previous situation (for a transition of the same strength), and it is then possible to achieve electroweak baryogenesis in scenarios where the gravitational wave signal may be detectable at BBO for moderately strong phase transitions (solid red lines in Figure 4) or even marginally at LISA for extremely strong transitions (dashed red lines in Figure 4).

VI. CONCLUSIONS.

If the electroweak phase transition is of first order, it will proceed by bubble nucleation and expansion. In the presence of a compression wave in front of the expanding bubble walls (which always occurs if the bubbles expand subsonically and can also occur under certain conditions if the bubbles expand supersonically), the relative velocity between the wall and the plasma in front (v_+) is smaller than V_w . While this effect is small for weak phase transitions (for which one gets $v_+ \simeq V_w$), it becomes important as the phase transition gets stronger, and for rather strong transitions one has $v_+ \ll V_w$. Since the background velocity of the plasma relevant for the electroweak baryogenesis process is v_+ whereas the relevant velocity for gravitational wave production through bubble collisions is V_w (see however [10]), this opens the possibility of achieving viable electroweak baryogenesis (satisfying the diffusion bound $v_+ \lesssim 0.15 - 0.3$) and a

sizable gravitational wave signal in the same scenario, which was previously regarded as not possible due to the very different ranges of wall velocities V_w that were thought to be required for each the two processes to be efficient. We actually find that in electroweak baryogenesis scenarios, the gravitational wave signal can be easily detected by BBO for moderately strong phase transitions ($\alpha_N \sim \mathcal{O}(0.2 - 0.3)$), and is very close to the LISA sensitivity curve for extremely strong transitions ($\alpha_N \sim \mathcal{O}(1)$).

However, whereas a moderately strong first order phase transition is a natural possibility in many theories beyond the Standard Model (and so a positive signal at BBO is plausible in these scenarios), the occurrence of such a strong transition as to observe a signal with LISA is quite unlikely since it corresponds to a very fine-tuned scenario, and also in this last case the bubble expansion would have to proceed through hybrids ($V_w > c_s$) and it has been argued that hybrids are not in general stable solutions, but may evolve into detonations [17]. One should have all these issues in mind when dealing with a concrete model.

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